

<name>

Class: Honors Geometry

Date: <date>

Topic: Lesson 8-2 (Similar Polygons)

Similar polygons

1. Corresponding \angle 's are \cong
2. Corresponding sides are proportional.

Symbol: \sim

Example

1. $\triangle ABC \sim \triangle XYZ \dots$ complete each statement:
($m\angle X = 42^\circ, m\angle Y = 78^\circ$)

a. $m\angle B = ?$ $\angle B$ corresponds to $\angle Y$ so $m\angle B = 78^\circ$

b. $\frac{BC}{YZ} = \frac{?}{XZ}$ \overline{XZ} corresponds to \overline{AC} so $\frac{BC}{YZ} = \frac{AC}{XZ}$

Similarity ratio

Ratios of lens of all corr. sides are equal. If $\triangle ABC \sim \triangle FED$

then $\frac{AB}{FE} = \frac{BC}{ED} = \frac{AC}{FD}$ (the corr sides are proportional)

Examples

2. **Problem #8, pg 425:** Are the polygons similar? If so, give the similarity stmt & similarity ratio. If not, explain.

Flip $QRST$ over (top-bottom) so QT is on the top.

Correspondence:

$\angle Q \cong \angle X, \angle T \cong \angle Y$ and $\angle S \cong \angle Z, \angle R \cong \angle W$ (**corr \angle 's \cong**)
and $\overline{QR} \& \overline{XW}, \overline{ST} \& \overline{ZY}, \overline{QT} \& \overline{XY}, \overline{RS} \& \overline{WZ}$

Similarity ratio: $\frac{QR}{XW} = \frac{ST}{ZY} = \frac{6}{8} = \frac{3}{4}$ or 3:4

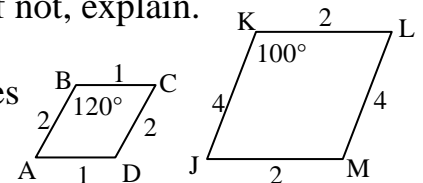
$$\frac{QT}{XY} = \frac{7.5}{10} = \frac{7\frac{1}{2}}{10} = \frac{\frac{15}{2}}{\frac{10}{1}} = \frac{15 \cdot 1}{2 \cdot 10} = \frac{15}{20} = \frac{3}{4} \text{ or } 3:4$$

$$\frac{RS}{WZ} = \frac{12}{16} = \frac{3}{4} \text{ or } 3:4 \text{ (corr sides proportional)}$$

Similar: $QRST \sim XWZY; \frac{3}{4}$ or 3:4

3. Are the parallelograms similar? If so, give the similarity statement and similarity ratio. If not, explain.

No; while corresponding sides are proportional ($\frac{1}{2}$), corr angles are not congruent.



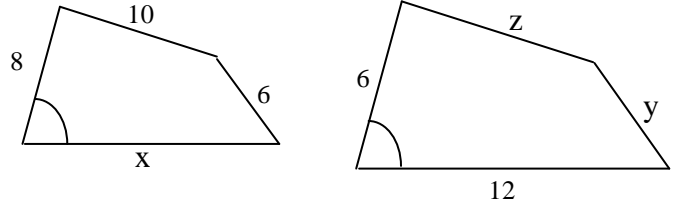
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4. **Problem #15, pg 426:** The polygons are similar. Find the value of ea var.



Match corr. sides in ratios going fm the smaller polygon to the larger. **Keep the order consistent!**

$$\frac{8}{6} = \frac{x}{12} = \frac{6}{y} = \frac{10}{z} \text{ (Note where the variables are)}$$

Now solve for each variable:

$$\frac{x}{12} = \frac{8}{6}; x = \frac{12 \cdot 8}{6} = 16 \quad \& \quad \frac{6}{y} = \frac{8}{6}; \frac{y}{6} = \frac{6}{8}; y = \frac{6 \cdot 6}{8} = 4.5 \quad \&$$

$$\frac{10}{z} = \frac{8}{6}; \frac{z}{10} = \frac{6}{8}; z = \frac{10 \cdot 6}{8} = 7.5$$

So $x = 16$; $y = 4.5$; $z = 7.5$

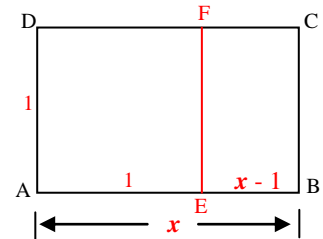
Golden rectangle

Rect w/len to width ratio of 1.618:1

Divides rect into square & smaller rect...sm rect ~ larger rect

Golden ratio

$$1.618:1 \text{ (or } \frac{l}{w} = \frac{1.618}{1} \text{ or } \frac{l}{w} = \frac{w}{l-w} \text{ or } \frac{l}{w} = \frac{l+w}{l} \text{)}$$



Example

The len & width of a rectangular tabletop are in the golden ratio. The shorter side is 40 in. Find the length of the longer side.

Let width $w = 40$ & len be l . Form a golden ratio proportion:

$$\frac{l}{w} = \frac{1.618}{1} = \frac{l}{40} \text{ and solve for } l.$$

$$\frac{l}{40} = \frac{1.618}{1}; l = 40 \cdot 1.618 = 64.72 \approx 65in$$